Minnesota State High School Mathematics League





Issue #7 September 4, 2018

A message from the Executive Director, Tom Young

Hello! Welcome back to another school year and another year of Math League competition!

This newsletter wraps up the 2017 - 2018 season, specifically the Summer Math Institute and the Coaches Conference, and looks forward to the 2018 - 2019 Math League season. Please read the newsletter thoroughly. You never know what tidbits of information you'll pick up.

The biggest change this year will be virtual sections. In a special May board meeting, the League approved this new method for qualifying for the State Tournament. The virtual sections will be finalized this fall at the September 30th board meeting. See the proposal below.

I applaud your commitment to high quality mathematics in the state of Minnesota!

Go Math League!

A message from Tom Kilkelly, Head of the Problem Writing Team

The problem writing team is well on its way in creating and vetting the problems for the 2018 - 2019 season. The team hopes to have all the meets, including the State Tournament, polished by the end of September.

We'd like to welcome our new problem writer Michael Tang. He joins the writing team of Mike Swenson, Jim Walker, Don Barry, Tom Kilkelly, and Martha Knutson.

Some Pictures from the 2018 Summer Math Institute



2018 Summer Math Institute

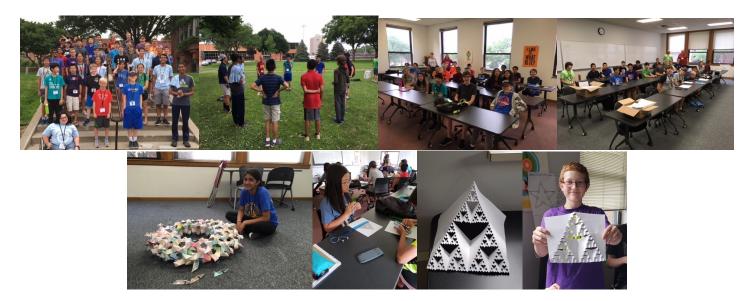
Each year, the Math League creates a Summer Math Institute for students entering $7^{\text{th}} - 9^{\text{th}}$ grade, and also entering $10^{\text{th}} - 12^{\text{th}}$ grade. This year's sessions were Advanced Problem Solving Techniques (7 - 9) and Counting Techniques (10 - 12).

Thanks go out to our teachers Stephanie Hegman, Leah Higginbotham, Carraig Hegi, and Ken Suman!! They were ably assisted by problem solving session teachers Dave Anderson, Julie Hasling, Heather Krumwiede, and Lewis Istok. And also making the experience great for our 40 students were RAs Nibir Sarma, Ashley Parent, Alex Pan, and Kelton Holsen.

Look for more information in subsequent newsletters about the 2019 sessions. Tentatively they are:

7–9 Mathematics and Art

10 – 12 Theory of Equations



2018 Coaches Conference

Each summer, the Math League sponsors a coaches conference to consult coaches on League business, teach the coaches new mathematical techniques, and provide coaches the opportunity to get to know each other.

On Thursday this year, Steven Dunbar was our guest speaker. Steven is the director of the AMC Competition and he led sessions on Geometry in competitive mathematics.

Thursday night, the attendees gathered together for dinner and a friendly, yet competitive, session of Escape Room. Friday morning was devoted to League business, teacher tidbits, coding of problems for our database, and exploration of the new math web site, Classpad.net.



Two Teacher Tidbits (presented at the Coaches Conference)

Look for more to come in subsequent newsletters!

1. A shortcut for changing repeating decimals to fractions

 $\frac{a}{b} = \frac{\text{Whole decimal-nonrepeating part}}{\text{"Whole place"} - \text{"nonrepeating place"}} \text{ subtract 1 in the denominator if the entire decimal repeats}$

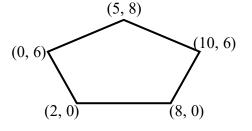
For example
$$0.\overline{6} = \frac{6-0}{10-1} = \frac{6}{9} = \frac{2}{3}$$

For example $0.8\overline{47} = \frac{847 - 8}{1000 - 10} = \frac{839}{990}$

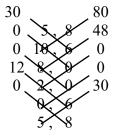
2. A shortcut for finding the area of a polygon (known as surveyor's method or shoelace method)

Given a polygon with its coordinates (see figure at right)

Start with one coordinate pair and write it down Continue with others (in a clockwise or ccw direction) and return to original pair



Connect the numbers with diagonals as shown and find the products



SUM the products on each side and take half the absolute value of the difference

$$\left|\frac{(30+12) - (80+48+30)}{2}\right| = 58$$
 This is the area of the polygon

See https://en.wikipedia.org/wiki/Shoelace_formula

Looking forward to this year, here is the motion that passed unanimously last May

Motion for moving to three tiers:

Move that, for the purpose of qualifying for the State Tournament, the schools in the league be organized into three tiers as outlined below. Each proposed tier is composed of 8 evenly-distributed virtual sections from different geographic regions across the state.

- a. The highest scoring team from each section is invited to the state tournament. In addition, 2 wild card teams per tier are invited to the state tournament. The wild card teams are the two highest scoring teams in the Tier that didn't win a section.
- b. Therefore, 10 teams from each Tier receive automatic bids. Thirty teams are thusly invited to the state tournament. The rest of the tournament field is filled out by choosing the next 6 to 10 highest scoring teams from across the state (regardless of Tier) for a full state tournament complement of 38 teams.
- c. The Hibbing Rule would be eliminated as a method for making it to the state tournament.
- d. The use of the alpha, beta, and gamma system at the state tournament would be eliminated. Teams would compete in the tier to which they are assigned.
- e. Placement of teams into tiers shall be based on enrollment numbers from the Minnesota State High School League for the upcoming two-year cycle. Tier assignments would be for two-year cycles, beginning with the 2019-2020 season; the 2018-2019 tier assignments will be only for one year. Adjustments in tiers are made based on the averages of the previous two years of performances. Tier 2 and 3 teams who average in the top 15 (overall) in the regular season in the previous two years would be moved to Tier 1 for the following two years. Tier 3 teams who average in the top 50 in the regular season in the previous two years of the previous two years would be moved to Tier 2 for the following two years. Initial placement of teams for the 2018-2019 season will be based on results of the 2016-2017 and 2017-2018 seasons.
- f. Teams that have been moved to a higher tier will be returned to their original tier if the 2-year review dictates it. The teams will be moved to their original tier if, during the two years they were moved to a higher tier, they did not maintain the standard by which they were moved up. For instance, if a tier 2 or tier 3 team was moved to tier 1 due to being in the top 15 (average over 2 years) but did not maintain that top 15 regular season average, the team would be returned to tier 2 or, correspondingly, tier 3. Also, if a tier 3 team was moved to tier 2 due to being in the top 50, but did not maintain the top 50 status for the two years they were moved up, the team would be moved back to tier 3.
- g. Any school will have the option "play up" to a higher Tier. Initial tier placements will be released by October 1 of the beginning of the two-year period. Teams must declare their intent to "play up" prior to October 15.
- h. Placement of schools added to the League in the middle of a tier assignment cycle shall be at the discretion of the Executive Committee or its designee.

Further, be it moved that the large school tier, Class 3A, be composed of the following schools

Class 3A Section 1

Century HS John Marshall HS Mayo HS Lakeville Schools Cotter HS Rosemount HS Apple Valley HS Owatonna HS

Class 3A Section 2

Shakopee Sr HS Eden Prairie HS Minnetonka Senior Edina HS Wayzata HS The Blake School St Louis Park HS

Class 3A Section 3

Park HS East Ridge HS Eagan HS Eastview HS St Thomas - Visitation Woodbury HS Henry Sibley HS Harding HS

Class 3A Section 4

North St Paul HS Central HS Roseville Area HS Stillwater Area HS White Bear Lake HS Tartan HS Highland Park HS St Paul Academy

Class 3A Section 5

Champlin Park HS Park Center Senior HS Armstrong HS Maple Grove Senior Osseo Senior HS Rogers HS Mounds View HS

Class 3A Section 6

Blmngtn Jefferson HS Minneapolis South HS Southwest HS Washburn HS Kennedy HS Hopkins HS Burnsville HS

Class 3A Section 7

Anoka HS Blaine HS Spring Lake Park HS Coon Rapids HS Andover HS Elk River HS Irondale HS

Class 3A Section 8

Moorhead HS St.Johns Prep Duluth East HS Cambridge-Isanti HS St Michael-Albertville Sauk Rapids-Rice HS Tech HS Buffalo HS

Move that the middle-sized school tier, Class 2A, be composed of the following schools

Class 2A Section 1

Austin HS Faribault HS Red Wing HS Northfield HS Osceola HS Waseca HS Stewartville HS Shattuck St.M

Class 2A Section 2

Hutchinson HS Delano St. Peter HS Dassel-Cokato HS Mankato West HS Mankato East HS Marshall HS

Class 2A Section 3

Simley HS South St Paul HS Johnson HS Hill Murray HS Como Park HS Washington Tech HS Mahtomedi HS

Class 2A Section 4

Minnehaha Academy Holy Family Catholic Cretin-Derham Hall Richfield HS Roosevelt HS Mound Westonka HS Orono HS

Class 2A Section 5

Columbia Heights HS Fridley HS DeLaSalle HS Patrick Henry HS St. Anthony Village HS Totino-Grace HS Edison HS Academy Holy Angels

Class 2A Section 6

Big Lake HS Cooper HS Foley HS Monticello HS Apollo HS Int. Sch MN/Eg Ridge Benilde-St Margaret's

Class 2A Section 7

Grand Rapids HS Hibbing HS Chisago Lakes HS North Branch HS Cloquet HS Duluth Denfeld HS Marshall School Hermantown HS

Class 2A Section 8

Bemidji Alexandria Area HS Detroit Lakes HS Fergus Falls HS Thief River Falls HS Sartell HS Rocori Sauk Rapids-Rice

Move that the small-sized school tier, Class 1A, be composed of the following schools

Class 1A Section 1

Lake City Chatfield HS Dover-Eyota HS LaCrescent-Hokah HS Lewiston-Altura HS Plview-Elgin-Millville St Charles HS Wabasha/Kellogg HS

Class 1A Section 2

Fulda HS Fairmont HS Blue Earth Area HS Lke Crystl/Wlcm Mem MN Valley Lutheran Jackson County Central HS Tri-City United HS

Class 1A Section 3

New London-Spicer Adrian HS Lakeview HS Luverne Jr Sr HS Montevideo HS MACCRAY HS BOLD HS

Class 1A Section 4

Providence Academy Hope Academy Parnassus Prep Humboldt HS Mounds Park Acad. St Croix Lutheran St. Paul Preparatory

Class 1A Section 5

Lourdes HS Zumbrota-Mazeppa Cannon Falls HS Kenyon-Wanamingo Triton HS Pine Island HS Goodhue HS

Class 1A Section 6

Breckenridge HS Pelican Rapids HS Albany HS Cathedral HS Atwtr-Csms-Grve City Park Rapids HS Nevis HS

Class 1A Section 7

Barnum HS Esko HS Moose Lake HS Willow River HS Mora HS Proctor HS Carlton HS East Cntral Secondary

Class 1A Section 8

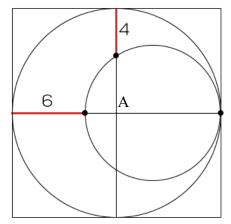
Badger HS Grnbush-Middle River Mesabi East HS Mt. Iron-Buhl HS International Falls HS Eveleth-Gilbert HS North Woods HS follow us on Facebook "Minnesota State High School Mathematics League" @MNSHSML and Twitter @MNHSMathLeague



A solution to the problem from Newsletter 6

Old Problem: https://math.stackexchange.com/questions/658449/interesting-geometry-problem-square-and-two-circles

Given a square with center A, and two circles as drawn, what is the area of the square?



Sol	ution:
30	ution.

If a is half of the side then with the power of the point of the middle point and with respect to smaller circle we have:

 $(a-6)a=(a-4)^2 \Rightarrow a=8 \Rightarrow Area=16^2=256$

New Problem

http://www.universityofcalicut.info/SDE/VI%20Sem.%20B.Sc%20Maths%20-%20Additional%20Course%20in%20lie%20of%20Project%20-Theory%20of%20equations%20&%20fuzzy%20set.pdf

If $\alpha + \beta + \chi = 1$, $\alpha^2 + \beta^2 + \chi^2 = 2$, and $\alpha^3 + \beta^3 + \chi^3 = 3$ Find $\alpha^4 + \beta^4 + \chi^4$