

# Appendix D: Regular Season Meet Topic Quick Reference

Each meet can contain topics from the previous meets.

## 1A Prealgebra Topics

- Fractions to add and express as the quotient of two relatively prime integers
- Complex fractions and continued fractions
- Decimals, repeating decimals
- Percentage, interest, and discount
- Least common multiple, greatest common divisor
- Number bases; change of base

## 1B Angles and Special Triangles

- The Theorem of Pythagoras; familiar Pythagorean triples
- Complementary, supplementary, and vertical angles
- Interior and exterior angles for triangles and polygons
- Angles formed by transversals cutting parallel lines
- Properties of isosceles and equilateral triangles
- Relationships in  $30^\circ$ - $60^\circ$ - $90^\circ$  and  $45^\circ$ - $45^\circ$ - $90^\circ$  triangles

## 1C Elementary Trigonometry

- Definitions and solution of right triangles
- Elementary identities
- Radian measure and graphs of elementary functions
- Trigonometric functions of multiples of  $\pi/6$ ,  $\pi/4$ ,  $\pi/3$ ,  $\pi/2$ .

## 1D Roots of Quadratic and Polynomial Equations

- Solution of quadratic equations by factoring, by completing the square, by formula
- Complex roots of quadratic equations; the discriminant and the character of the roots
- Relations between roots and coefficients
- Synthetic Division
- Function notation

## 2A Linear Equations in One Unknown

- Solving numeric equations (perhaps involving a second degree term which drops out)
- Solving literal equations
- Story problems leading to linear equations in one variable
- Linear inequalities
- Absolute value equations and inequalities

## 2B Triangular figures and solids

- Medians, angle bisectors, and altitudes
- Ceva's and Stewart's Theorems
- Area of a triangle (including Hero's Formula)
- Triangular prisms & pyramids (including volume and surface area)

## 2C Trigonometry

- Functions of sums of angles and sums of functions of angles
- Half and double angle formulas
- Reduction formulas

## 2D Analytic Geometry of Straight Lines and Circles

- Slope, families of parallel, perpendicular, or coincident lines
- Point-slope, slope-intercept, intercept, normal forms of the straight line
- Intersections (solution of simultaneous systems)

## 3A Systems of Linear Equations in Two (or on occasion three) Variables

- Numeric and literal systems
- Relation to graphical procedures
- Word problems leading to such systems
- Systems of inequalities used to define a region in the plane
- Determinants

## 3B Polygonal figures and solids

- Special quadrilaterals and regular polygons (including area formulas) 12
- Intersecting diagonals
- Circumscribed polygons and Ptolemy's Theorem
- Polygonal prisms & pyramids (including volume and surface area)

## 3C Trigonometry

- Law of sines, law of cosines
- Inverse functions and their graphs
- Solving trigonometric equations
- De Moivre's Theorem and the roots of unity
- Complex numbers in the complex plane

## 3D Exponents and Logarithms

- Use of fractional, negative exponents
- Simplifying expressions involving radicals
- Solving equations involving radicals
- Use of logarithms; identities involving logarithms
- Solving logarithmic equations
- Relationships between logarithms to different bases

## 4A Algebraic Manipulation

- Factoring (including  $x^3 + y^3$  and  $x^3 - y^3$ )
- Sums, products, quotients of rational expressions
- Solving equations (including radical equations) involving these skills, but ultimately solvable by factoring or the quadratic formula (but no complex roots)
- Rational exponents
- Simplifying radical expressions
- Function notation and variational dependencies (inverse and direct variation)

## 4B Circular figures and solids

- Central, inscribed, tangential, and exterior angles
- Power of a point (chords, secants, tangents) x Interior and exterior tangents of two circles x Intercepted arcs
- Area of circles, sectors, circular segments
- Cylinders, cones, & spheres (including volume and surface area)

## 4C Miscellaneous Topics

- Sequences: patterns and recursion formulas, arithmetic and geometric sequences
- Series: partial sums, formulas for  $1 + 2 + \dots + n$ ,  $1^2 + 2^2 + \dots + n^2$ , and  $1^3 + 2^3 + \dots + n^3$
- Function notation; factorial notation and the Binomial Theorem

## 4D Analytic Geometry of the Conic Sections

- Using the standard forms of equations of the conic sections
- Graphs, including the location of foci, directrices, and asymptotes
- Use of properties of conics to solve applied problems, including max-min for parabolas

## 5A Puzzle Problems (20 minutes)

- Word problems, one or more variables
- Max-min problems not requiring calculus
- Problems found in "brain-teaser" type books
- Logic puzzles, including the use of Venn Diagrams

## 5B Congruence and Similarity

- Ratio and proportion
- Segments intercepted by parallel lines
- Identification of similar/congruent figures
- Ratios of areas and volumes
- Elementary trigonometric ratios

## 5C Counting and Probability

- Permutations, with and without replacement
- Combinations, with and without replacement
- Using the principle of inclusion, exclusion
- Using the binomial and multinomial expansions
- Nonnegative integer solutions to  $x_1 + x_2 + \dots + x_n = b$ .
- Definition, simple applications of probability (when to multiply, when to add)

## 5D Variations of the previous year's AMC 12 (contests A and B)